

The following LP is degenerate:

$$\text{Max } z = 5x_1 + 2x_2$$

$$\text{s.t. } x_1 + x_2 \leq 6$$

$$x_1 - x_2 \leq 0$$

$$x_1, x_2 \geq 0$$

(When a LP is equal to zero, don't use simplex method)

Z	$x_1$	$x_2$	$s_1$	$s_2$	RHS	Ratio
1	-5	-2	0	0	0	
0	1	1	1	0	6	6 = (6/1)
0	(1)	-1	0	1	0	0 = (0/1)

1	0	-7	0	5	0	
0	0	(2)	1	-1	6	3 = (6/2)
0	1	-1	0	1	0	N/A

1	0	0	3.5	1.5	21	
					3	
					3	

$+s_n \leq b_i$   
 $-e_i \geq b_i$

$$\text{Min } z = 2x_1 + 3x_2$$

$$\text{s.t. } 0.5x_1 + 0.25x_2 \leq 4$$

$$x_1 + 3x_2 \geq 20$$

$$x_1 + x_2 = 10$$

Row 0	2	-2x <sub>1</sub>	-3x <sub>2</sub>	= 0
Row 1		0.5x <sub>1</sub>	+ 0.25x <sub>2</sub> + s <sub>1</sub>	= 4
Row 2		x <sub>1</sub>	+ 3x <sub>2</sub> - e <sub>2</sub>	= 20
Row 3		x <sub>1</sub>	+ x <sub>2</sub>	= 10

Z	$x_1$	$x_2$	$s_1$	$e_2$	
	-2	-3	0	0	
	0.5	0.25	1	0	
	1	3	0	-1	$= -e_2 = 20$
	1	1	0	0	$e_2 = -20$

↳ must be  $\geq 0$

Z	$x_1$	$x_2$	$s_1$	$e_2$	$a_2$	$a_3$	RHS
	-2	-3	0	0	0	0	
	0.5	0.25	1	0	0	0	4
	1	3	0	-1	1	0	20 ✓
	1	1	0	0	0	1	10

Intro into the "Big M" method

- Max problem, look at smallest number for ratio
- Min problem, look at biggest number for ratio

URS - unrestricted in sign (can't use simplex method)

$$x_1 \geq 0$$

$$x_2 \text{ URS} \rightarrow \text{Let } x_2 = x_2' - x_2''$$

$$x_2' \geq 0$$

$$x_2'' \geq 0$$