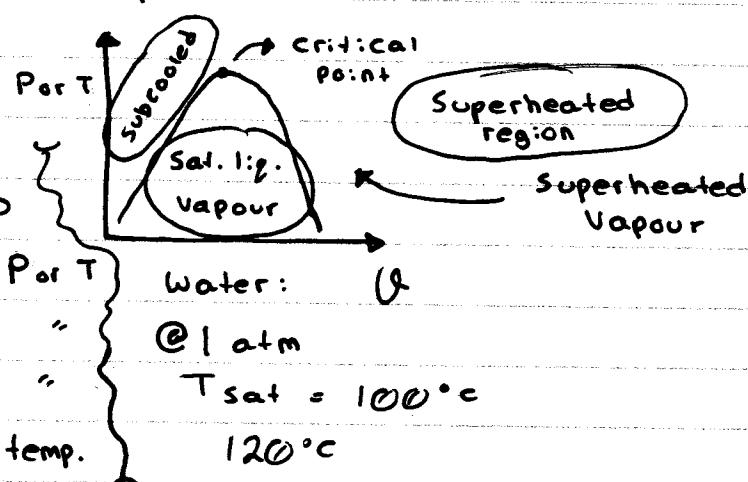


# Thermo Chapter 3 : Properties of Pure Substance

## Superheated Vapor

### Properties (Superheated)

- 1)  $T > T_{\text{sat}} @ \text{given } P$
- 2)  $\vartheta > \vartheta_f @ \text{given } P_{\text{or }} T$
- 3)  $U > U_f @ 1 \text{ atm}$
- 4)  $h > h_f @ T_{\text{sat}} = 100^\circ\text{C}$
- 5)  $P < P_{\text{sat}} @ \text{given temp. } 120^\circ\text{C}$



### Properties (Subcooled)

- 1)  $T < T_{\text{sat}} @ \text{given } P$
- 2)  $\vartheta < \vartheta_f @ \text{given } P \text{ and } T$
- 3)  $U < U_f @ P_{\text{sat}} > P$
- 4)  $h < h_f @ P_{\text{sat}} > P$
- 5)  $P > P_{\text{sat}} @ \text{given temp.}$

$\vartheta, u, h$

$T \quad P$

$120^\circ\text{C} @ 1 \text{ atm } (101 \text{ kPa})$

$\hookrightarrow P_{\text{sat}} (199 \text{ kPa})$

$(P_{\text{sat}} > P)$

## Reference State and Reference Value : $\vartheta, u, h, s$

For water @  $0^\circ\text{C}$   $u = 0$

$s = 0$

For refrigerant 134a  $\rightarrow$  ref state  $-40^\circ\text{C}$

### Ideal gen. eq'n of state:

$$\textcircled{1} \text{ Boyle's Law} \rightarrow \vartheta \propto 1/P \quad [T = \text{const}]$$

$$\textcircled{2} \text{ Charles Law} \rightarrow \vartheta \propto T \quad [P = \text{const}]$$

$$\boxed{P, \vartheta, T} \quad \vartheta \propto \frac{1}{P} \times T \quad [\text{P and T varied}]$$

$$\vartheta \propto T/P \rightarrow P\vartheta \propto T$$

$K \rightarrow$  depends on mass and type

$$\rightarrow P\vartheta = KT$$

If mass = 1 kg  $\rightarrow P\vartheta = RT$

$$R_{\text{air}} = 287 \text{ J/kg}\cdot\text{K}$$

$$= 0.287 \text{ kJ/kg}\cdot\text{K}$$

$$\left[ R = \frac{P\vartheta}{T} = \frac{N_A}{m} \times \frac{m^2}{kg} \times \frac{1}{K} \right]$$

$$= 3 / \text{kg}\cdot\text{K}$$

(2)

$$P\vartheta = RT$$

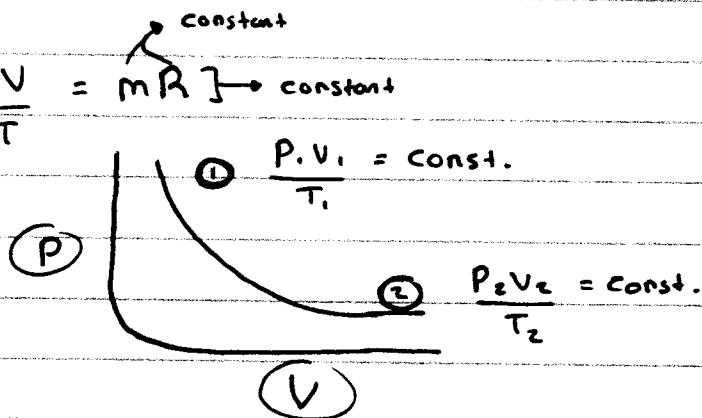
$$P\left(\frac{V}{m}\right) = RT \quad \xrightarrow{\text{constant}} \quad \frac{PV}{T} = mR \quad \xrightarrow{\text{constant}}$$

$$\therefore PV = mRT \quad \xrightarrow{\text{total volume}}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$P\vartheta = RT$$

$$PV = mRT$$



Compressibility Factor : (z)

$$Z = \frac{PV}{RT}$$

$$P\vartheta = ZRT$$

P<sub>a</sub> or T<sub>a</sub>

↳ reduced pressure  
↳ reduced temp

$$P_a = P/P_{cr}$$

$$T_a = T/T_{cr}$$

$$Z = 1 \quad (\text{:ideal gas})$$

$$Z \neq 1 \quad (\text{real gas})$$

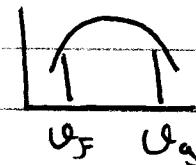
Example 3-5 : (from textbook)

$$V = 80 \text{ L}, m = 4 \text{ kg}$$

$$U = \frac{V}{m} = \frac{80}{4 \times 1000} = 0.02 \text{ m}^3/\text{kg}$$

Table A-12

$$@160 \text{ kPa} : U_s$$



$$U_f = 0.0007435 \text{ m}^3/\text{kg}$$

$$U_g = 0.12355 \text{ m}^3/\text{kg}$$

∴ refrigerant 134a is in

Sat. liquid vapor region

$$T = T_{sat} @ 160 \text{ kPa} = -15.60^\circ\text{C}$$

$$\text{b) Quality} = \vartheta - U_f + x U_{fg}$$

$$\therefore x = \frac{\vartheta - U_f}{U_{fg}} = \frac{\vartheta - U_f}{U_g - U_f}$$

$$x = 0.157$$

c) Enthalpy ↴

## c) Enthalpy

$$h = h_f + xh_{fg}$$

$$= 31.18 \text{ kJ/kg} + 0.157 \times 209.96 \text{ kJ/kg}$$

$$\therefore h = 64.1 \text{ kJ/kg}$$

## d) Vapor Vol.

$$x = \frac{m_g}{m_f} \quad \therefore m_g = x m_f$$

$$= 0.157 \times 4 \text{ kg}$$

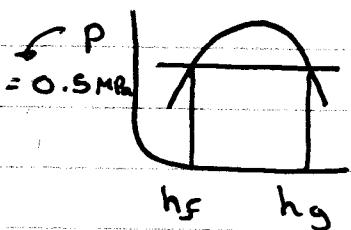
$$= 0.628 \text{ kg}$$

$$V_g = \frac{V_g}{m_g} \quad \therefore V_g = V_g \times m_g = 0.6 \times 0.12335$$

$$= 0.0736 \text{ m}^3$$

$$= 77.62 \text{ vapor}$$

Example 3-7:  
From table A-5



## Chapter 4: Energy Analysis of Closed Systems

Thermal Sci.

- obj: 1) Moving boundary work
- 2) Energy balance for closed system
- 3) Specific heats
- 4) Int. energy, enthalpy + s.p. heats of ideal gas, solid, liquid.

Work = Force × distance

$$\delta W = F \times ds$$

$$= PA ds$$

$$= P du \quad \text{↑ vol}$$

$$\text{press. } P = F/A$$

$$\therefore F = PA$$

∴ Total work for process 1-2:

$$W_b = \int_1^2 P du$$

$$1) V = \text{Const.}$$

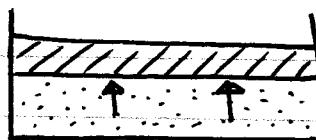


$$P dV = 0$$

$$\therefore \delta W = 0$$

$$W_b = 0$$

$$2) P = \text{const.}$$



$$\delta W_b = \int_1^2 P dV$$

$$= P \int_1^2 dV$$

$$W_b \Rightarrow P(V_2 - V_1)$$

$$\Rightarrow W_b = P(V_2 - V_1)$$

$$Q \rightarrow \text{sp. vol}$$

$$Q = \frac{V}{m}$$

$$V = mQ$$

$$3) \text{ Isothermal process (ideal gas)}$$

$$T = \text{const.}$$

$$\text{Boyle's Law : } T = C ; V \propto \frac{1}{P}$$

$$V = \text{const.} = C$$

$$\therefore P = C/V \rightarrow ①$$

$$PV = C = P_1 V_1 = P_2 V_2 \rightarrow ②$$

$$PV = mRT \rightarrow ③$$

$$W_b = \int_1^2 P dV = \int_1^2 \frac{C}{V} dV = C \int_1^2 \frac{dV}{V} = C [\ln V_2 - \ln V_1]$$

$$= C \ln \frac{V_2}{V_1}$$

$$W_b = P_1 V_1 \ln \left( \frac{V_2}{V_1} \right)$$

(2)

## Polytropic Process:

$$PV^n = C \quad \text{or} \quad n \neq 1$$

$$\hookrightarrow P = CV^{-n} \quad | \quad W_b = \int_1^2 P dV = \int_1^2 CV^{-n} dV$$

$$= C \int_1^2 V^{-n} dV$$

$$\Rightarrow C \left[ \frac{V_2^{-n+1} - V_1^{-n+1}}{-n+1} \right]$$

$$\boxed{W_b = \frac{P_2 V_2 - P_1 V_1}{1-n}}$$

$$PV = mRT$$

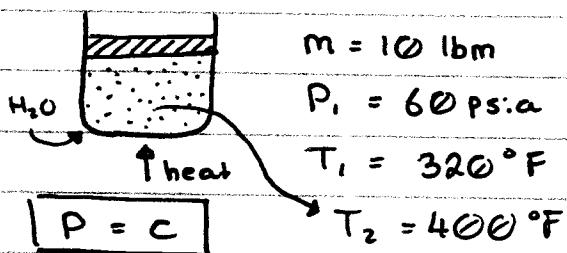
$$C = P_1 V_1^n = P_2 V_2^n$$

$$\boxed{W_b = \frac{mR(T_2 - T_1)}{1-n}}$$

$$U_1 = @60 \text{ psia}, 320^\circ\text{F}$$

$$U_2 = @80 \text{ psia}, 400^\circ\text{F}$$

Example 4-2:



$$m = 10 \text{ lbm}$$

$$P_1 = 60 \text{ psia}$$

$$T_1 = 320^\circ\text{F}$$

$$T_2 = 400^\circ\text{F}$$

$$W_b = mP(U_2 - U_1)$$

$$= 10 \times 60 (8.3549 - 7.4363)$$

$$= (1 \text{ lbm}) (1 \text{ b}\text{f}/\text{in}^2) (\text{ft}^3/\text{lbm})$$

$$= 76038 (\text{ft.lbf})$$

TABLE A6E

Example 4-3:

$$W_b = P_1 V_1 \ln \frac{V_2}{V_1}$$

$$= 100 \text{ kPa} \times 0.4 \text{ m}^3 \times \ln \frac{0.1 \text{ m}^3}{0.4 \text{ m}^3}$$

$$= -555 \text{ kJ}$$

$$= \text{kPa} \times \text{m}^3$$

$$= \frac{\text{KN}}{\text{m}^2} \times \cancel{\text{m}^3} (\text{m})$$

$$= \text{kJ}$$

## Energy balance for closed systems

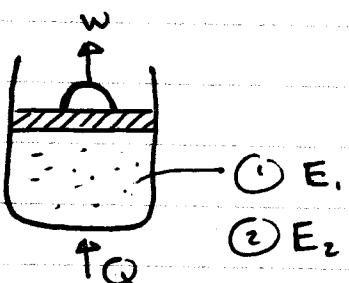
$$E_{in} - E_{out} = \Delta E_{system}$$

$$E_{in} - E_{out} = \frac{d}{dt} E_{sys}$$

$$\dot{Q} = Q - \Delta t$$

$$\dot{W} = W / \Delta t$$

$$dE/dt = \Delta E / \Delta t$$



$$E_1 + Q = E_2 + W$$

$$\therefore Q - W = \Delta E$$

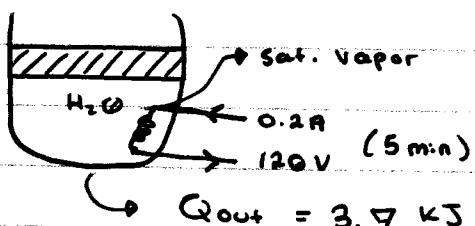
↳ general form of

1st law of thermodynamics

$$Q_{net,in} - W_{net,out} = \Delta E$$

$$\therefore Q - W = \Delta U$$

Example 4-5:



$$P_1 = P_2 = 300 \text{ kPa}$$

$$m = 25 \text{ g}$$

$$Q - W = \Delta E = \Delta U + \boxed{\Delta KE + \Delta PE}$$

$$Q - W = \Delta U$$

$$Q - (W_b + W_{other}) = U_2 - U_1$$

$$Q - P(V_2 - V_1) - W_{other} = U_2 - U_1$$

$$Q - W_{other} = (U_2 + P_2 V_2) - (U_1 + P_1 V_1)$$

$$H = U + PV \quad \therefore Q - W_{other} = H_2 - H_1 = \Delta H$$

$$-3.7 \text{ kJ} - 7.2 \text{ kJ} =$$

TABLE A-5

$$P_1 = 300 \text{ kPa}$$

$$P = VI$$

$$h_1 = h_g @ 300 \text{ kPa}$$

$$W_e = V I \Delta t$$

$$= 2724.9 \text{ kJ/kg}$$

$$= 120V \times 0.2R$$

$$-3.7 + 7.2 = (0.025)(h_2 - 2724.9)$$

$$\times 5 \times 60$$

$$h_2 = 2864.9 \text{ kJ/kg}$$

$$= 7.2 \text{ kJ}$$

$$T_2 = 200^\circ\text{C} \quad (\text{Example 4-6}) \quad h_2 = 2864.9 \text{ kJ/kg}$$