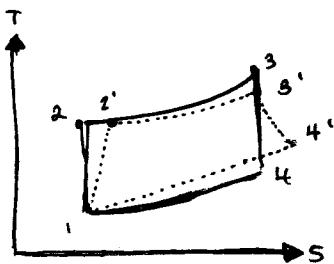


(1)

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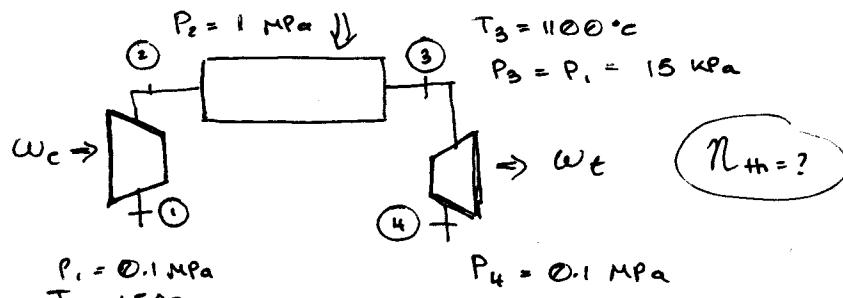
$$\text{back work} = \frac{W_c}{W_t}$$

In Brayton Cycle, the compressor might require 40 to 80% of the output of the Turbine.

In Rankine Cycle, 1 or 2% of the turbine work is required to drive the pump.

(10.2)

Example



$$W_{ca} = h_2 - h_1$$

$$\eta_c = \frac{W_{cs}}{W_{ca}} = \frac{h_{2s} - h_1}{h_{2a} - h_1} = \frac{C_p(T_{2s} - T_1)}{C_p(T_{2a} - T_1)} \quad (I)$$

(isentropic)
(actual)

$$\frac{T_{2s}}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{k-1}{k}} \Rightarrow T_{2s} = (15 + 273.2) \left(\frac{1}{0.1}\right)^{\frac{0.4}{1.4}}$$

$\boxed{T_{2s} = 556.8 \text{ K}}$

$$\text{From (I): } 0.8 = \frac{556.8 - 288.2}{T_{2a} - 288.2} \rightarrow \boxed{T_{2a} = 624 \text{ K}}$$

$$W_{ca} = C_p(T_{2a} - T_1) = (1.004)(624 - 288.2) = 337 \text{ kJ/kg}$$

$$W_{ta} = h_3 - h_{4a} = C_p(T_{3a} - T_{4a})$$

$$\eta_T = \frac{W_{ta}}{W_{ts}} = \frac{h_3 - h_{4a}}{h_3 - h_{4s}} = \frac{C_p(T_{3a} - T_{4a})}{C_p(T_{3s} - T_{4s})} \quad (II)$$

$$\frac{T_3}{T_{4s}} = \left(\frac{P_3}{P_4}\right)^{\frac{k-1}{k}} \rightarrow \boxed{T_{4s} = 713.9 \text{ K}}$$

$$\text{From (II): } 0.85 = \frac{1373 - T_{4a}}{1373 - 713.9} \rightarrow \boxed{T_{4a} = 812.8 \text{ K}}$$

$$W_{ta} = C_p(T_3 - T_{4a}) = 1.004 (1373.2 - 812.8)$$

$$W_{ta} = 562.4 \text{ kJ/kg}$$

2 (continued)

2

$$W_{net} = W_{Ta} - W_{ca} = 562.4 - 337 = 225.4$$

$$\eta_{BW} = \frac{W_{ca}}{W_{Ta}} = \frac{337}{562.4} = 0.6 \Rightarrow 60\%$$

$$\eta_{th} = \frac{W_{net}}{q_n} = \frac{225.4}{...}$$

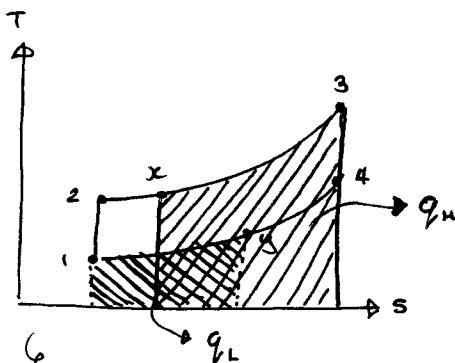
$$q_n = h_3 - h_{2a} = C_p(T_3 - T_{2a}) = (1.004)(1373.2 - 624) \\ = 751.8 \text{ kJ/kg}$$

$$\eta_{th} = \frac{W_{net}}{q_{hs}} = \frac{W_{Ts} - W_{Cs}}{q_{hs}} = \frac{C_p(T_3 - T_{4s}) - C_p(T_{2s} - T_s)}{C_p(T_3 - T_{2s})}$$

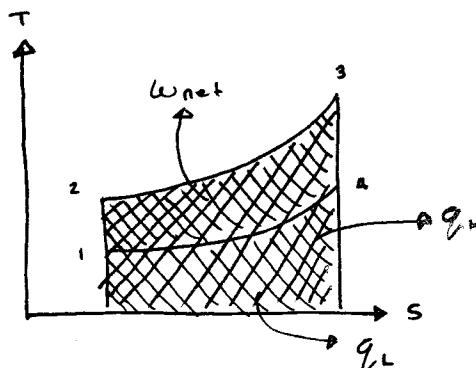
$$\eta_{ths} = \frac{T_3 - T_{4s} - T_{2s} + T_1}{T_3 - T_{2s}} = \frac{1373.2 - 713.9 - 556.8 + 288.2}{1373.2 - 556.8}$$

$$\eta_{ths} \approx 48\%$$

/end



With regeneration



the efficiency of this cycle w/ regeneration

$$\eta_{th} = \frac{W_{net}}{q_n} = \frac{W_e - W_c}{q_n}$$

$$q_n \approx C_p(T_3 - T_X)$$

$$W_e \approx C_p(T_3 - T_H)$$

For an ideal regenerator, $T_H = T_X$, $\therefore q_n = W_e$

$$\rightarrow \eta_{th} = 1 - \frac{T_1}{T_3} \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} = 1 - \frac{T_1}{T_3}$$

(1)

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$$\begin{array}{ll}
 \textcircled{1} \quad 10 \text{ kPa} & \Rightarrow h_1 = 191.8 \frac{\text{kJ}}{\text{kg}} \\
 \text{Sat. 1: } & \\
 \textcircled{2} \quad 0.5 \text{ MPa} & \Rightarrow h_2 = 192.3 \frac{\text{kJ}}{\text{kg}} \\
 \textcircled{3} \quad 0.5 \text{ MPa} & \Rightarrow h_3 = 640.09 \frac{\text{kJ}}{\text{kg}} \\
 \text{Sat. 1: } & \\
 \textcircled{4} \quad 15 \text{ MPa} & \Rightarrow h_4 = 643.92 \frac{\text{kJ}}{\text{kg}} \\
 \textcircled{5} \quad 15 \text{ MPa} & \\
 \textcircled{6} \quad 4 \text{ MPa} & \Rightarrow h_6 = 1087.4 \frac{\text{kJ}}{\text{kg}} \\
 \text{Sat. 1: } & \\
 \textcircled{7} \quad 15 \text{ MPa} & \Rightarrow h_7 = 1101.2 \frac{\text{kJ}}{\text{kg}} \\
 \textcircled{8} \quad 15 \text{ MPa} & \\
 \textcircled{9} \quad 15 \text{ MPa} & \Rightarrow h_9 = 3582 \frac{\text{kJ}}{\text{kg}} \\
 600^\circ\text{C} & \\
 \textcircled{10} \quad 4 \text{ MPa} & \Rightarrow h_{10} = 3155 \frac{\text{kJ}}{\text{kg}} \\
 \textcircled{11} \quad 4 \text{ MPa} & \Rightarrow h_{11} = 3674.9 \frac{\text{kJ}}{\text{kg}} \\
 600^\circ\text{C} & \\
 \textcircled{12} \quad 0.5 \text{ MPa} & \Rightarrow h_{12} = 3014.8 \frac{\text{kJ}}{\text{kg}} \\
 \textcircled{13} \quad 10 \text{ kPa} & \Rightarrow h_{13} = 2337.7 \frac{\text{kJ}}{\text{kg}} \\
 & \\
 S_g = S_{10}, \quad S_{11} = S_{12} = S_{13} & \\
 \dot{m}_{11} = (1-y) \dot{m}_{10} & \\
 \dot{m}_6 = y \dot{m}_{10} & \\
 \dot{m}_{11}/\dot{m}_{12} = 1-y/z &
 \end{array}$$

$$\rightarrow V_1 = 0.00101$$

$$w_{p1} = V_1(P_2 - P_1)$$

$$\Rightarrow (0.00101)(500 - 10) = 0.4949$$

$$w_p = h_2 - h_1 \rightarrow h_1 = 192.3 \frac{\text{kJ}}{\text{kg}}$$

$$\rightarrow w_{p2} = h_4 - h_3 \rightarrow w_{p2} = V_3(P_4 - P_3)$$

$$\rightarrow w_{p3} = h_7 - h_6 \rightarrow w_{p3} = V_6(P_7 - P_6)$$

$$\rightarrow S_{10} = S_g = 6.6775 \quad (\text{superheated}) \quad (\text{interpolate})$$

$$\rightarrow S_{12} = S_{11} = 7.3688 \quad (\text{interpolate})$$

$$\begin{aligned}
 \rightarrow S_{13} &= S_{12} = S_{11} = 7.3688 & h_f &= 191.8 & \left. \begin{aligned} S_F &= 0.6492 \\ S_{Fg} &= 7.5010 \end{aligned} \right\} \\
 && h_{fg} &= 2392.82
 \end{aligned}$$

$$S_{13} = S_f + x_{13} S_{Fg}$$

$$7.5010 = 0.6492 + x_{13}(7.5010)$$

$$h_{13} = h_f + x_{13} h_{fg}$$

$$h_{13} = 191.81 + (0.8958)(2392.82)$$

$$h_{13} = 2335.7 \frac{\text{kJ}}{\text{kg}}$$

(2)

C. FWH:

$$y h_{10} + (1-y) h_5 = (1-y) h_5 + y h_6$$

mixer:

$$h_8 = (1-y) h_5 + y h_7 \quad \textcircled{II}$$

$$\text{For ideal CFWH} \Rightarrow h_6 = h_5 = 1087.4 \text{ kJ/kg}$$

$$\text{From } \textcircled{I} \text{ and } \textcircled{II} : y = 0.1766$$

$$h_8 = 1089.8$$

O. FWH:

$$z h_{12} + (1-y-z) h_2 = (1-y) h_3$$

$$z = 0.1306$$

→ 10.3

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Example

$$\dot{Q}_H = h_3 - h_x$$

$$T_4 = T_x = ?$$

$$T_4/T_3 = \left(P_4/P_3 \right)^{\frac{k-1}{k}} \Rightarrow T_4 = 710.8 \text{ K}$$

1373.2

$$\dot{Q}_H = C_p (T_3 - T_x) = 1.0004 (1373.2 - 710.8)$$

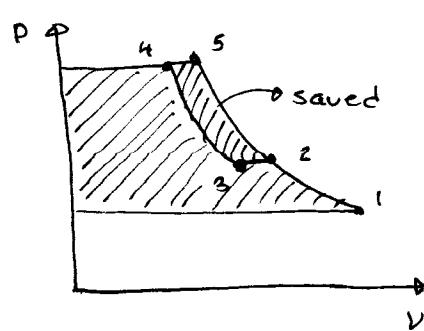
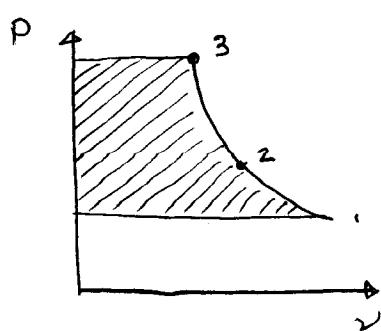
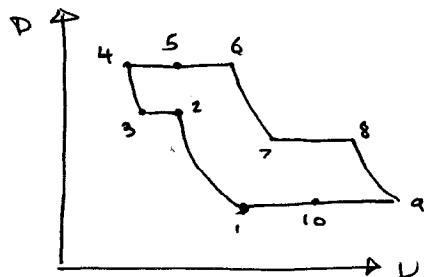
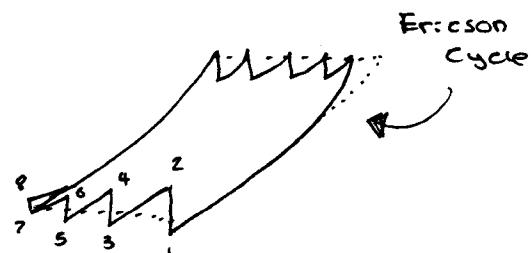
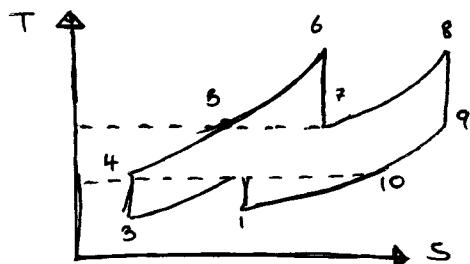
$$\dot{Q}_H = 664.7 \text{ kJ/kg}$$

From previous example:

$$\dot{W}_{\text{net}} = 395.2 \text{ kJ/kg} \quad \rightarrow \quad \eta_{\text{th}} = \frac{395.2}{664.7} = 59.5 \%$$

$$\eta_{\text{th, without ref.}} = 48.2 \%$$

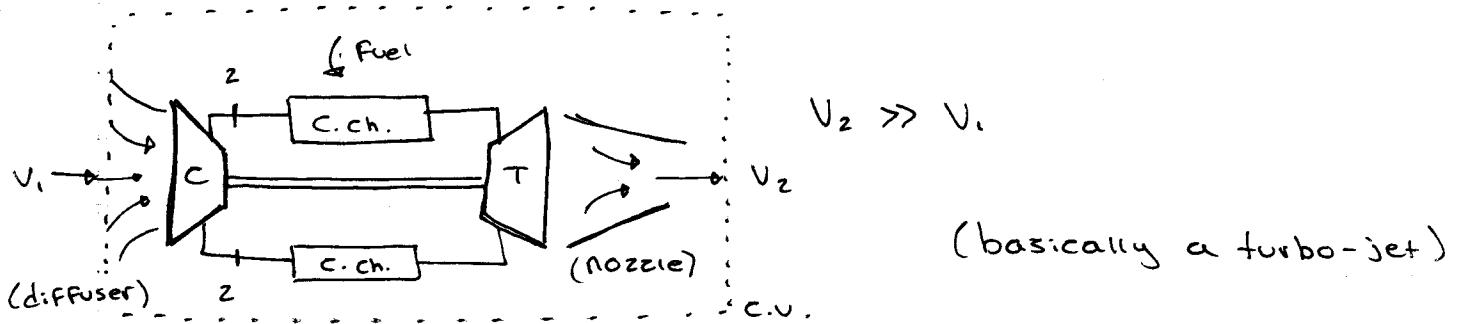
Gas turbine Power-Cycle Configuration



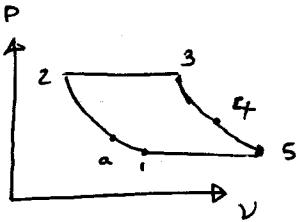
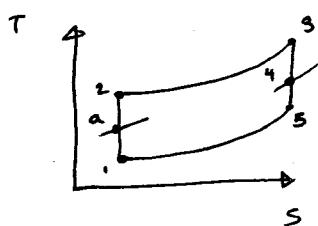
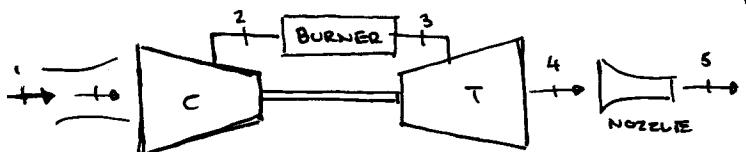
(with intercooler)

$$W = - \int V dP$$

(2)



Air-Standard Cycle for Jet Propulsion



Example:

Consider an ideal jet propulsion cycle in which air enters the compressor at 0.1 MPa and 15°C ...

$$P_1 = 0.1 \text{ MPa}$$

$$T_1 = 288.2 \text{ K}$$

$$P_2 = 1 \text{ MPa}$$

$$T_2 = 556.8 \text{ K}$$

$$\left(\frac{T_2}{T_1}\right) = \left(\frac{P_2}{P_1}\right)^{\frac{\kappa-1}{\kappa}}$$

$$\begin{aligned} w_c &= C_p(T_2 - T_1) = (1.004)(556.8 - 288.2) \\ &= 269.5 \text{ kJ/kg} \end{aligned}$$

$$P_3 = 1 \text{ MPa}$$

$$w_c = w_t = 269.5$$

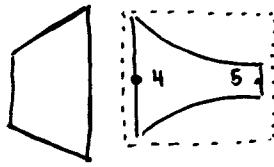
$$T_3 = 1373.2 \text{ K}$$

$$w_t = C_p(T_3 - T_4) \Rightarrow 269.5 = (1.004)(1373.2 - T_4)$$

$$T_4 = 1104.6 \text{ K}$$

$$\left(\frac{T_4}{T_3}\right) = \left(\frac{P_4}{P_3}\right)^{\frac{\kappa-1}{\kappa}} \Rightarrow P_4 = 0.4668 \text{ MPa}$$

3



$$\cancel{q} + h_4 + \frac{V_4^2}{2} + gZ_4 = \cancel{q} + h_5 + \frac{V_5^2}{2} + gZ_5$$

$$h_4 = h_5 + \frac{V_5^2}{2}$$

$$\frac{T_5}{T_4} = \left(\frac{P_5}{P_4} \right)^{\frac{k-1}{k}} \Rightarrow T_5 = 710.8 \text{ K}$$

(x1000)

$$V_5^2 = 2C_p(T_4 - T_5) = 2(1.004)(1104.6 - 710.8)$$

$$\rightarrow V_5 = 889 \text{ m/s}$$